## Deadlock Avoidance of Flexible Manufacturing Systems by Colored Resource-Oriented Petri Nets With Novel Colored Capacity

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## Overview

(1) Research Background
(2) Colored capacity

## CROPN

## Creator

The concept of colored resource-oriented petri nets (CROPN) is proposed by Professor Wu's work.

## feature 1

resource-oriented modeling method

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feature 2
colors and capacity
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## CROPN modeling method



## process plan

Part types $A$ and $B$. Plane for $A: r_{1} \rightarrow r_{2}$. Plane for $B: r_{1} \rightarrow r_{2} \rightarrow r_{3}$

## resource-oriented

place $p_{1}$ for $r_{1}, p_{2}$ for $r_{2}$, and $p_{3}$ for $r_{3}$.

## CROPN color



## color

Token with color $t_{i} \in T$ can only enable transition $t_{i}$.

## notation

We use $M(p, t)$ to represent the number of tokens with color $t$ in place $p$ at marking $M$.

## CROPN color assumption



## Remark

The work in Professor Wu assume that the color of a token will changed when this token goes from a place to another and the change of color is decided by a process plan and is known in advance.

For instance, for part $B: p_{1} \rightarrow p_{2} \rightarrow p_{3}:$ token $\left(p_{1}, t_{2}\right) \rightarrow$ token $\left(p_{2}, t_{3}\right) \rightarrow$ token $\left(p_{3}, t_{4}\right)$.

## CROPN capacity



Figure: A simple example for illustration

## capacity

We use $K(p)$ to denote the number of tokens the place $p$ can hold.

## CROPN

## Control policy

To forbid bad markings.

## Realization

To add control places to the net

## Ideal of this paper

We introduce color into capacity and define the colored capacity to realize the given control policy without adding control places.

## Colored capacity

## Feature

We introduce color into capacity. Then we can restrict number of token with specific color in a place.

## Colored capacity

Given a CROPN with marking $M$, let $K_{c}: P \times T \times M \rightarrow\{0,1, \ldots\}$ be the colored capacity such that for all $p \in P$, for all $t \in T$, for all marking $M$ reachable from the initial marking, $K_{c}(p, t, M)$ represents the maximum free number of tokens with color $t$ that $p$ can hold at marking $M$.

For instance, if we set $K_{c}\left(p_{1}, t_{1}, M\right)=1$, then the free space for token with color $t_{1}$ is one in place $p_{1}$ at marking $M$.

## CROPN control policy



## Setting

$t_{1} \rightarrow$ token with color $t_{3}$ or $t_{1}$ in place $p_{1} . K\left(p_{1}\right)=2, K\left(p_{2}\right)=1$.

## bad marking

$M\left(p_{1}, t_{1}\right)=2$ and $M\left(p_{2}, t_{2}\right)=1$.
control policy
$u_{1}: M\left(p_{1}, t_{1}\right)+M\left(p_{2}, t_{2}\right) \leq 2$.

## CROPN



## Control policy to be realized

$u_{1}: M\left(p_{1}, t_{1}\right)+M\left(p_{2}, t_{2}\right) \leq 2$.

## Colored capacity

$K_{c}\left(p_{1}, t_{1}, M\right)=2-M\left(p_{1}, t_{1}\right)-M\left(p_{2}, t_{2}\right)$.
If $M\left(p_{1}, t_{1}\right)=1$ and $M\left(p_{2}, t_{2}\right)=1$, then we have $K_{c}\left(p_{1}, t_{1}, M\right)=0$.

## Realization of control policy by colored capacity



## Colored capacity

$K_{c}\left(p_{1}, t_{1}, M\right)=2-M\left(p_{1}, t_{1}\right)-M\left(p_{2}, t_{2}\right)$.

## Contradiction

$M\left(p_{1}, t_{3}\right)=1$ and $M\left(p_{1}, t_{1}\right)=1, M\left(p_{2}, t_{2}\right)=0$, then we have $K_{c}\left(p_{1}, t_{1}, M\right)=1$, which contradicts $K\left(p_{1}\right)=2$.

## Realization of control policy by colored capacity



## Colored capacity

$K_{c}\left(p_{1}, t_{1}, M\right)=$ $\min \left[\left(2-M\left(p_{1}, t_{1}\right)-M\left(p_{2}, t_{2}\right)\right), K\left(p_{1}\right)-M\left(p_{1}, t_{1}\right)-M\left(p_{1}, t_{3}\right)\right]$

Thus if $M\left(p_{1}, t_{3}\right)=1$ and $M\left(p_{1}, t_{1}\right)=1, M\left(p_{2}, t_{2}\right)=0$, we have $K_{c}\left(p_{1}, t_{1}, M\right)=0$. Then we solve the contradiction above.

## Conclusion

## Remark 1

We do not consider how to obtain control policies.

## Remark 1

Colored capacity is marking-variant.

## Remark 2

Normal capacity:no color. Colored capacity:have color.

## Contribution of this paper

We introduce color into capacity and define the colored capacity to realize the given control policy without adding control places.

## Thanks

